

Analytical Chemistry, and Chemistry in General requires Constancy and Consistency

We as scientist are governed by immutable Laws.

1. Laws of Nature

2. Laws of Logic

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## Laws of Nature

- General:
  - Gravity
  - Electromagnetism
  - Strong Nuclear Forces
  - Weak Nuclear Forces
  - Quantum Mechanics
  - Relativity

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## Laws of Nature

### Specific:

| Symbol          | Definitions                                          |
|-----------------|------------------------------------------------------|
| $I$             | Quantity of radiation                                |
| $I_o$           | Quantity of incident radiation                       |
| $I_r$           | Quantity of reflected radiation                      |
| $I_t$           | Quantity of transmitted radiation                    |
| $I_a$           | Quantity of absorbed radiation                       |
| $n_1$           | Index of refraction of the surrounding medium        |
| $n_2$           | Index of refraction of the object                    |
| $\theta_i$      | Angle of incidence                                   |
| $\theta_t$      | Angle of transmitted ray                             |
| $K$             | Absorption coefficient as used in Beer-Lambert's Law |
| $L$             | Distance a light ray is propagated in a medium       |
| $R_{\perp}$     | Perpendicular component of reflected light           |
| $R_{\parallel}$ | Parallel component of reflected light                |

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## Laws of Logic

- Identity
- Law on Non-Contradiction

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## Identity

**Definitions:** Object Identity.

$$x = y =_{df}$$

$$(\mathcal{O}!x \ \& \ \mathcal{O}!y \ \& \ \Box \forall P (Px \equiv Py)) \ \vee \ (\mathcal{A}!x \ \& \ \mathcal{A}!y \ \& \ \Box \forall P (xP \equiv yP))$$

**Definitions:** Relation Identity.

$$.1) \ P = G =_{df} \ \Box \forall x (xP \equiv xG)$$

$$.2) \ P^n = G^n =_{df} \ (\text{where } n > 1)$$

$$\begin{aligned} \forall x_1 \dots \forall x_{n-1} ([\lambda y \ P^n y x_1 \dots x_{n-1}] = [\lambda y \ G^n y x_1 \dots x_{n-1}] \ \& \\ [\lambda y \ P^n x_1 y x_2 \dots x_{n-1}] = [\lambda y \ G^n x_1 y x_2 \dots x_{n-1}] \ \& \dots \ \& \\ [\lambda y \ P^n x_1 \dots x_{n-1} y] = [\lambda y \ G^n x_1 \dots x_{n-1} y]) \end{aligned}$$

$$.3) \ p = q =_{df} \ [\lambda y \ p] = [\lambda y \ q]$$

**Axioms:** Logic of Identity. Where  $\alpha, \beta$  are both individual variables, or both  $n$ -place relation variables ( $n \geq 0$ ), and  $\phi(\alpha, \beta)$  is the result of substituting one or more occurrences of  $\beta$  for  $\alpha$  in  $\phi(\alpha, \alpha)$  (provided  $\beta$  is substitutable for  $\alpha$  in the occurrences of  $\alpha$  it replaces), the modal closures of the following are logical axioms of our system:

$$\alpha = \beta \rightarrow [\phi(\alpha, \alpha) \equiv \phi(\alpha, \beta)]$$

Aristotle's Law of Identity

**Everything that exists has a specific nature.** ... Each entity exists as something specific, its identity is particular, and it cannot exist as something else. An entity can have more than one characteristic, but any characteristic it has is a part of its identity.

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## Law of Non-Contradiction

**Aristotle's contribution**

The traditional source of the law of non-contradiction is Aristotle's *Metaphysics* where he gives three different versions.

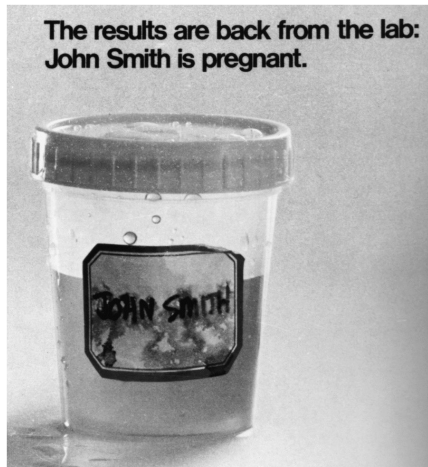
1. ontological: "It is impossible that the same thing belong and not belong to the same thing at the same time and in the same respect." (1005b19-20)
2. psychological: "No one can believe that the same thing can (at the same time) be and not be." (1005b23-24)
3. logical (aka the medieval Lex Contradictoriarum): "The most certain of all basic principles is that contradictory propositions are not true simultaneously." (1011b13-14)

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## The importance of reliable data!



*Exploring Chemical Analysis*, 3th Ed., D.C. Harris, WH Freeman, NY, 2005

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## Error in chemical analyses

- **Mean** (average, arithmetic mean)
  - Serves as the central “best” value for a set of replicate measurements
  - For a set of measurements,  $x_i$ , where  $i = 1, 2, 3, \dots$

$$\bar{x} = \frac{\sum_{i=1}^N x_i}{N} \quad \bar{x} = \text{mean}$$

- **Median**  $N = \text{number of measurements}$   
Is the middle result when the data are arranged in order of size
- Ideally, Mean = Median, but this is rarely true

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## Definitions

- **Replicates:**
  - Samples from the same system that are carried through an analysis in an identical manner
  - Forensic samples (e.g. blood) often taken in duplicates (think Olympics)
- **Error:**
  - Deviation of a result from the accepted true value

- **Precision:**

- Deviation of a result from the average of a set of results:

$$d_i = |x_i - \bar{x}|$$

 $d_i = \text{deviation of result } i$  $x_i = \text{result } i$  $\bar{x} = \text{mean}$ 

- **Accuracy:**

- Deviation of a result from the accepted true value

$$E_i = x_i - x_t$$

 $E_i = \text{error of result } i$  $x_i = \text{result } i$  $x_t = \text{"true" value}$ 

- Error can be determined in a single measurement; precision cannot

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## Definitions

- Absolute error:** has units & sign ( $\pm$ )  

$$E_i = x_i - x_t$$

$$E_i = \text{error of result } i$$

$$x_i = \text{result } i$$

$$x_t = \text{"true" value}$$
- Relative error:** error expressed as a percent & has a sign ( $\pm$ )

$$E_r = \frac{x_i - x_t}{x_t} \times 100\% = \text{percent error}$$

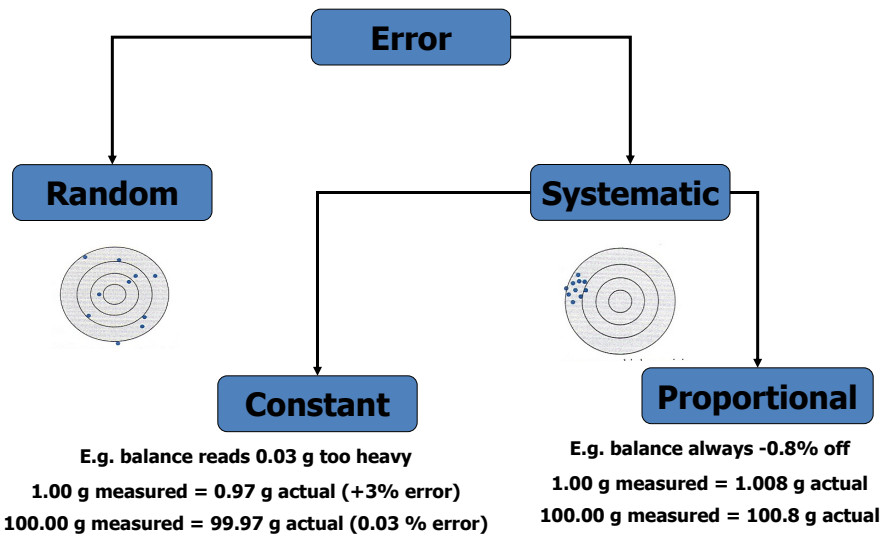
- Relative error can be expressed in ppt or ppm:

$$E_r = \frac{x_i - x_t}{x_t} \times 10^6 = \text{ppm error}$$

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## Types of errors



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## Systematic error

- Has definite value, assignable cause, and affects all replicates similarly
- Origins of systematic errors:
  - 1) Instrumental errors
    - faulty calibration
    - use outside appropriate range
    - instabilities in components
    - etc.
  - 2) Method error
    - unrepresentative sampling
    - incomplete chemistry
    - impure/unstable reagents

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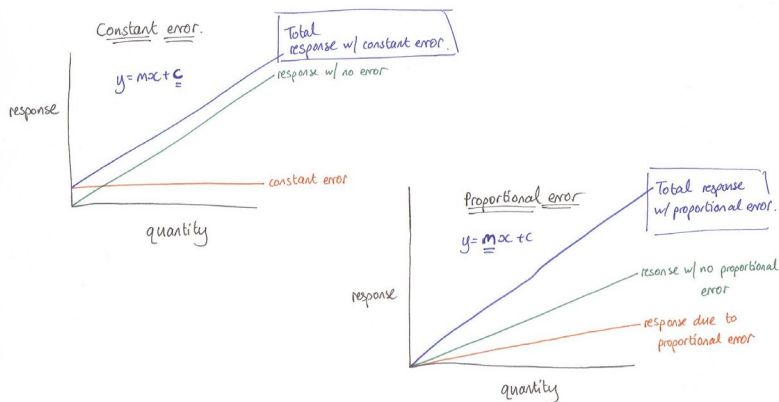
## Systematic error

- Has definite value, assignable cause, and affects all replicates similarly
- Origins of systematic errors:
  - 3) Operator errors
    - Misreading dials, scales, menisci
    - Poor control of conditions (temp, pH etc.)
    - Poor technique (e.g. blowout pipeting)
    - etc.

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## Constant v. proportional errors

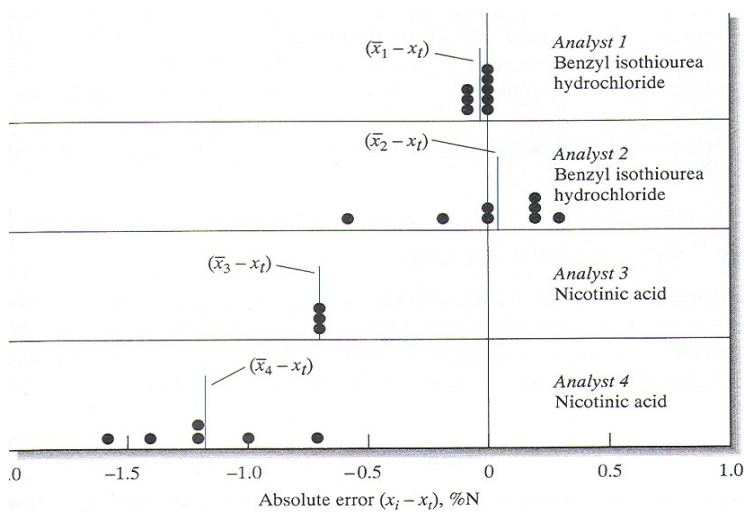


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## Accuracy and Precision

Analysis of nitrogen in two compounds by two different methods



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## Samples & populations

$\mu$  = mean value of the population (system)

$\bar{x}$  = estimate of  $\mu$ , because we only take small samples from the system

As  $n_{\text{sample}} \rightarrow N_{\text{population}}$ ,  $\bar{x} \rightarrow \mu$

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## Samples & populations

Precision of a population of data is described by population standard deviation,  $\sigma$  :

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (x_i - \mu)^2}{N}}$$

Precision of a sample of data is described by sample standard deviation,  $s$ :

$$s = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{\sum_{i=1}^N (d_i)^2}{n-1}}$$

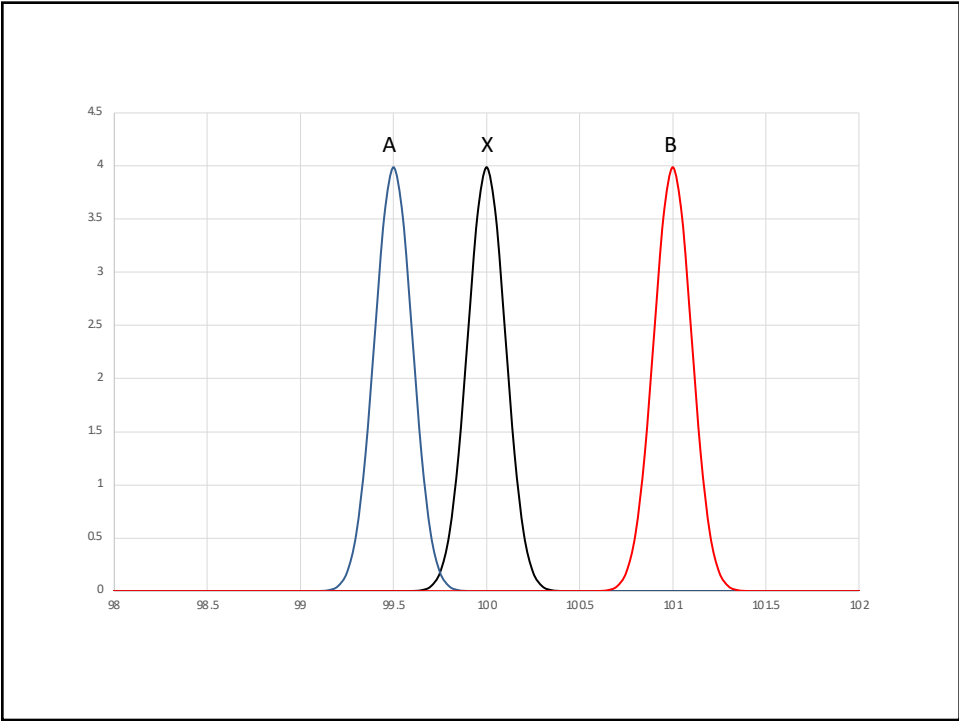
As  $n_{\text{sample}} \rightarrow N_{\text{population}}$ ,  $s \rightarrow \sigma$  just as  $\bar{x} \rightarrow \mu$

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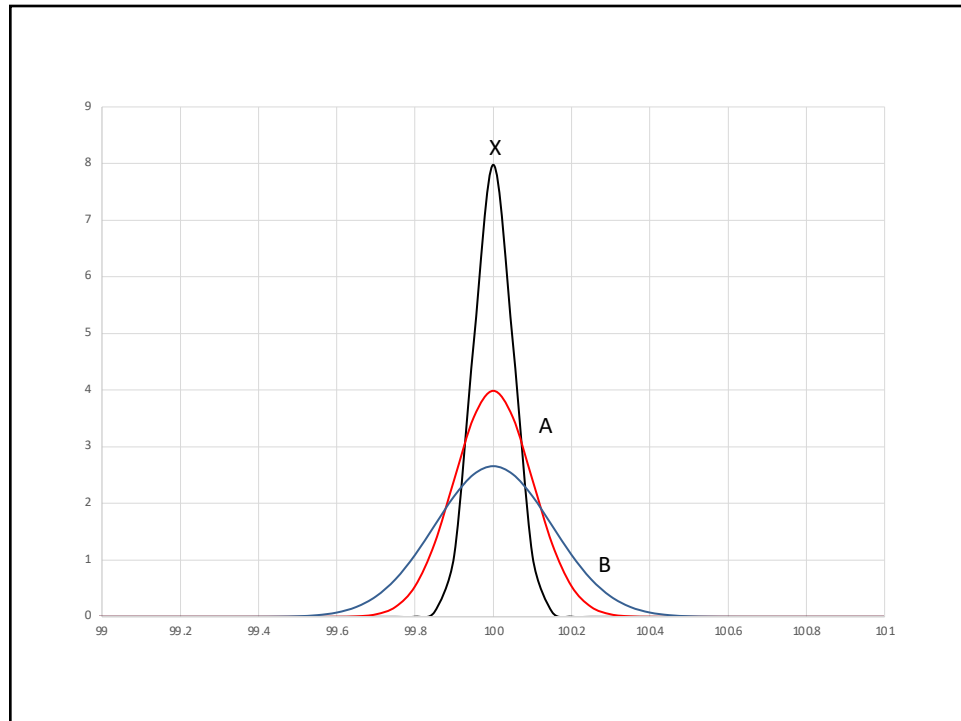
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| Description         | Equation                                                              | Variable                                                                          |
|---------------------|-----------------------------------------------------------------------|-----------------------------------------------------------------------------------|
| Arithmetic Mean     | $\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$                                | $x_i = \text{the } i\text{th value}$<br>$n = \text{total number of values}$       |
| Degrees of Freedom  | $v = (n - 1)$                                                         |                                                                                   |
| Variance            | $V(x) = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{v}$                     |                                                                                   |
| Standard Deviation  | $s = \sqrt{V(x)} = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{v}}$   |                                                                                   |
| Normal Distribution | $y(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ | $\mu = \text{population mean}$<br>$\sigma = \text{population standard deviation}$ |
| Confidence Limits   | $\mu = \bar{x} \pm t\left(\frac{s}{\sqrt{n}}\right)$                  | $t = \text{confidence interval value}$                                            |

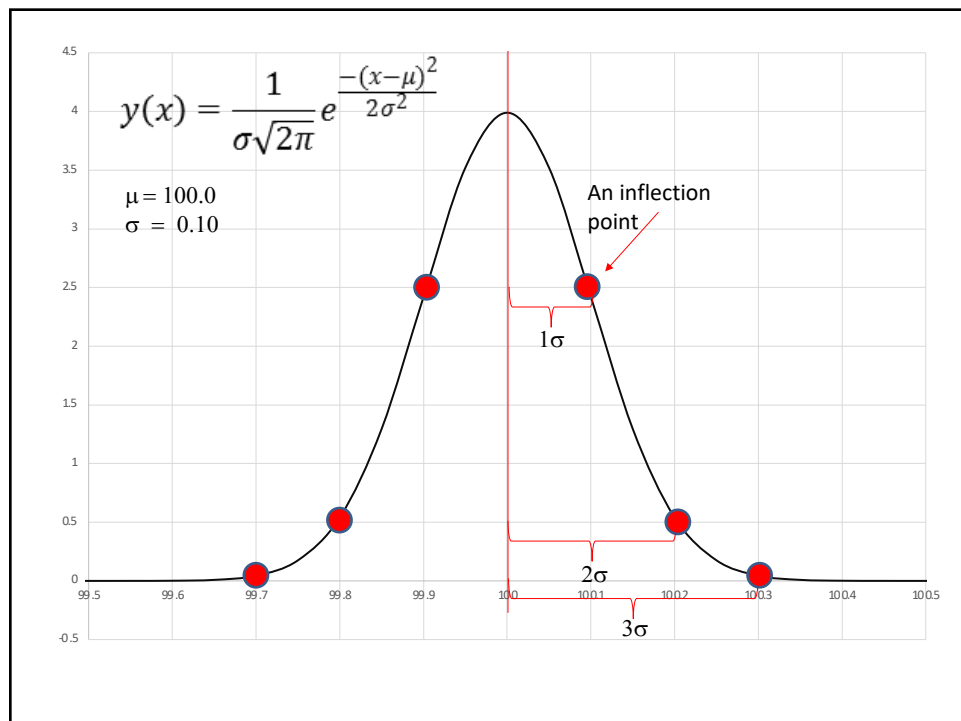
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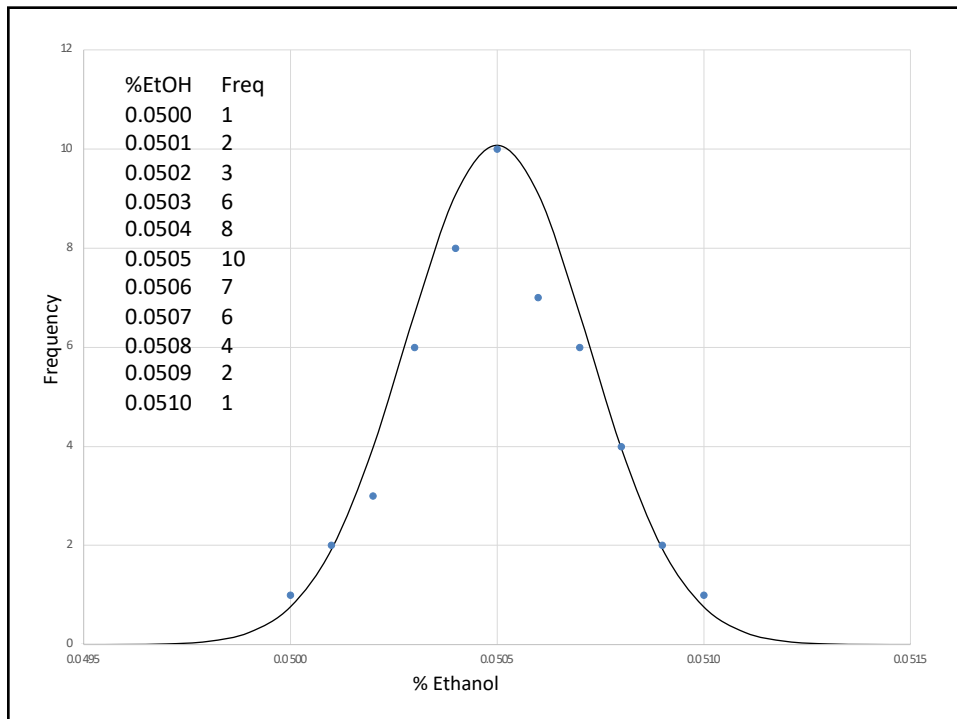
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t values for confidence intervals

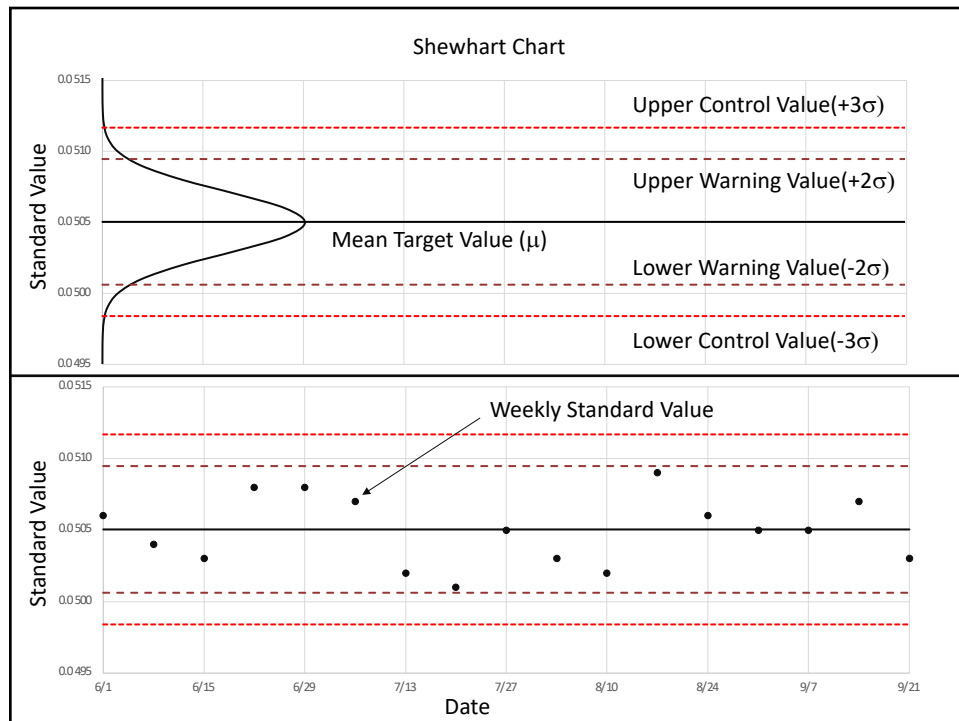
| V   | 95%   | 99%   |
|-----|-------|-------|
| 1   | 12.71 | 63.66 |
| 2   | 4.3   | 9.92  |
| 3   | 3.18  | 5.84  |
| 4   | 2.78  | 4.6   |
| 5   | 2.57  | 4.03  |
| 10  | 2.23  | 3.17  |
| 20  | 2.09  | 2.85  |
| 30  | 2.04  | 2.75  |
| 50  | 2.01  | 2.68  |
| 100 | 1.98  | 2.63  |

$$\mu = x \pm t\left(\frac{s}{\sqrt{n}}\right)$$

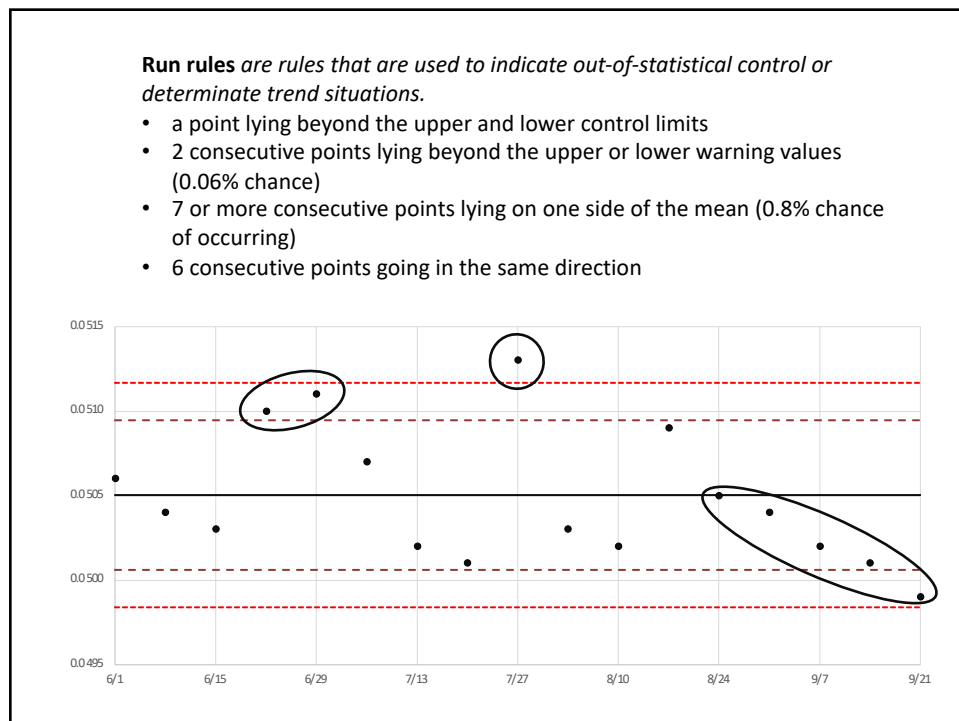
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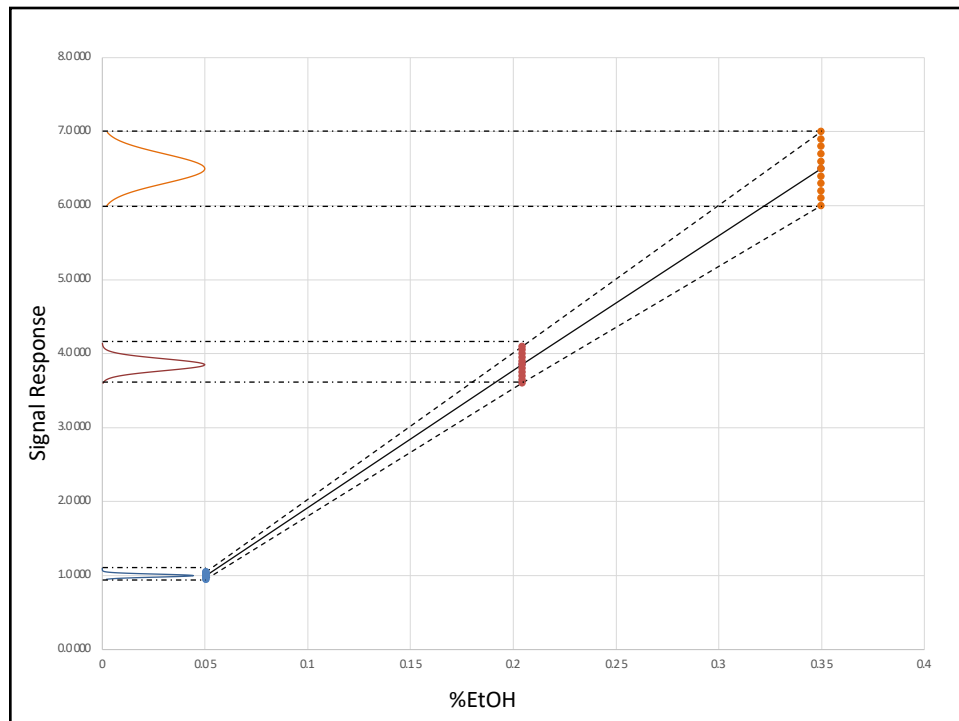
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### Comparing two experimental means

- This can be used to test
  - 1) whether two samples are significantly different
  - 2) whether two methods are significantly different
- We still use the T-test (and the t-tables)
- Different samples and different methods might have different standard deviations
  - This has to be accounted for by pooling the deviations of the means

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### Comparing two experimental means

$$\bar{x}_a - \bar{x}_b = \pm t s_{pooled} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}$$

$$\text{or, } t = \frac{\bar{x}_a - \bar{x}_b}{s_{pooled} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}}$$

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### Comparing two experimental means

$$\bar{x}_a - \bar{x}_b = \pm t s_{pooled} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}$$

$$\text{or, } t = \frac{\bar{x}_a - \bar{x}_b}{s_{pooled} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}}$$

$$s_{pooled} = \sqrt{\frac{s_1^2(n_1 - 1) + s_2^2(n_2 - 1) + \dots}{n_1 + n_2 \dots - \text{number data sets}}}$$

**If  $t > t_{crit}$  then reject the hypothesis that the means are the same.**

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# Data analysis and interpretation

- Data collected represented in a matrix

| Objects<br>going down<br>in different<br>rows | Variables going across in different columns |            |            |            |            |
|-----------------------------------------------|---------------------------------------------|------------|------------|------------|------------|
|                                               | X-var<br>1                                  | X-var<br>2 | X-var<br>3 | Y-var<br>1 | Y-var<br>2 |
| Sample 1                                      |                                             |            |            |            |            |
| Sample 2...                                   |                                             |            |            |            |            |

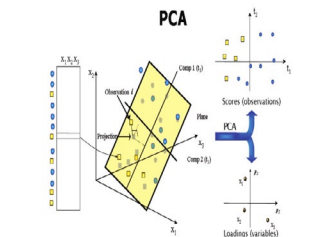
A propositional approach to describing and using metabolomics data (the x-data) for analyzing complex systems. These may have other specific properties (the y-data) which one may also wish to 'explain' in terms of the x-data.

- Chemometric Approach
  - Principle Component Analysis (PCA)
  - Soft Independent Modeling of Class Analogy (SIMCA)
  - Partial Least-Squares (PLS) Method by Projections to Latent Structures
  - Orthogonal PLS (OPLS)
- Targeted Profiling

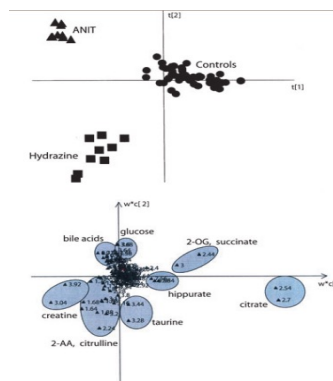
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## PCA

- Unsupervised
- Multivariate analysis based on projection methods
- Main tool used in chemometrics
- Extract and display the systematic variation in the data
- Each Principle Component (PC) is a linear combination of the original data parameters
- Each successive PC explains the maximum amount of variance possible, not accounted for by the previous PCs
- PCs Orthogonal to each other
- Conversion of original data leads to two matrices, known as scores and loadings
- The scores(T) represent a low-dimensional plane that closely approximates X. Linear combinations of the original variables. Each point represents a single sample spectrum.
- A loading plot/scatter plot(P) shows the influence (weight) of the individual X-variables in the model. Each point represents a different spectral intensity.
- The part of X that is not explained by the model forms the residuals(E)
- $X = TP^T = t_1p_1^T + t_2p_2^T + \dots + E$



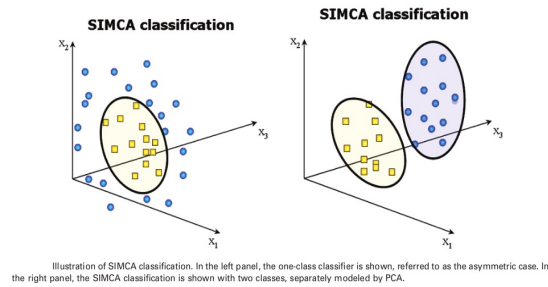
A principal component analysis (PCA) model approximates the variation in a data table by a low dimensional model plane. This model plane provides a score plot, where the relation among the observations or samples in the model plane is visualized. For example, if there are any groupings, trends, or outliers. The loading plot describes the influence of the variables in the model plane, and the relation among them. An important feature is that directions in the score plot correspond to directions in the loading plot, and vice versa.



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# SIMCA

- Supervised learning method based on PCA
- Construct a separate PCA model for each known class of observations
- PCA models used to assign the class belonging to observations of unknown class origin
- Boundaries defined by 95% class interval
- Recommended for use in one class case or for classification if no interpretation is needed



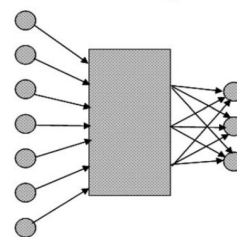
- One-class problem: Only disease observations define a class; control samples are too heterogeneous, for example, due to other variations caused by diseases, gender, age, diet, lifestyle, etc.
- Two-class problem: Disease and control observations define two separate classes

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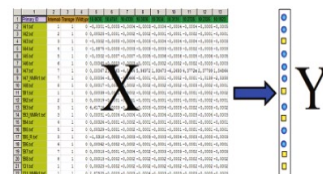
# PLS

- Supervised learning method.
- Recommended for two-class cases instead of using SIMCA.
- Principles that of PCA. But in PLS, a second piece of information is used, namely, the labeled set of class identities.
- Two data tables considered namely X (input data from samples) and Y (containing qualitative values, such as class belonging, treatment of samples)
- The quantitative relationship between the two tables is sought.
- $X = TP^T + E$
- $Y = TC^T + F$
- The PLS algorithm maximizes the covariance between the X variables and the Y variables
- PLS models negatively affected by systematic variation in the X matrix not related to the Y matrix (not part of the joint correlation structure between X-Y).

(a) Input data (b) Mathematical transformation(s) (c) Output classes

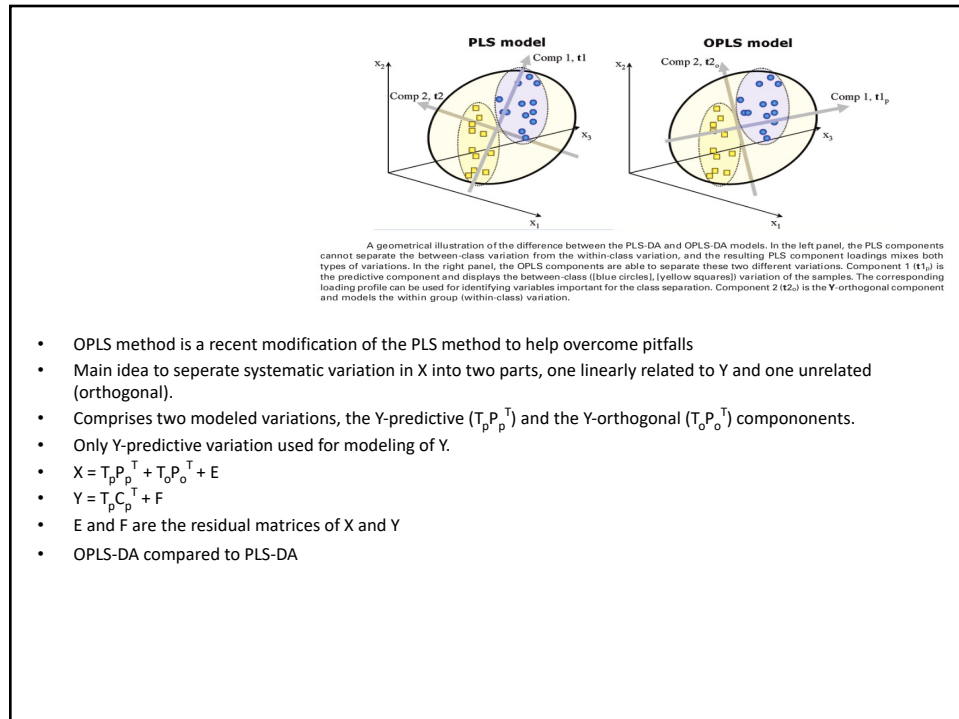


The class assignment problem. The inputs can be considered, and are referred to, as the "explanatory variables" or "x-data" whereas the functional or the other classes of interest, which are still variables associated with the samples, are referred to as "dependent variables" or "y-data" and are to be obtained as the outputs.



Class information can also be used to construct an additional matrix, hereinafter called the Y matrix, consisting of a discrete 'dummy' variable where [1]/[0] indicate the class belonging.

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## Remarks on pattern classification

- Intent in using these classification techniques not to identify specific compound
- Classify in specific categories, conditions or disease status
- Traditional clinical chemistry depended on identifying and quantifying specific compounds
- Chemometric profiling interested in looking at all metabolites at once and making a phenotypic classification of diagnosis

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## Targeted profiling

- Targeted metabolomic profiling is fundamentally different than most chemometric approaches.
- In targeted metabolomic profiling the compounds in a given biofluid or tissue extract identified and quantified by comparing the spectrum of interest to a library of reference spectra of pure compounds.
- Key advantage: Does not require collection of identical sets = More amenable to human studies or studies that require less day-to-day monitoring.
- Disadvantage: Relatively limited size of most current spectral libraries = bias metabolite identification and interpretation.
- A growing trend towards combining the best features of both chemometric and targeted methods.

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## Databases

- Large amount of data
- Need for databases that can be easily searched
- Better databases will help in combining chemometric and targeted profiling methods
- Newly emerging databases
- HMDB good model for other databases
- Challenge of standardisation

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